

TRIUMF



Introduction to

μ SR ^{otation}
^{elaxation}
^{esonance}

m
u
o
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s
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n

Applied^{*}
Elementary
Particle
Physics

- The World's μ SR Facilities
- Basic Techniques of μ SR
- Applications of μ SR
- Research Opportunities in μ SR

^{*}(to basic research in
Materials Science
and Chemistry)

Jess H. Brewer

UNBC, 26 March 2004

Visit our Web site!

<http://musr.org>

Where in the World is μ SR?

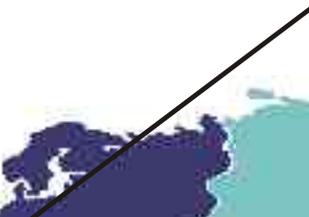
TRIUMF



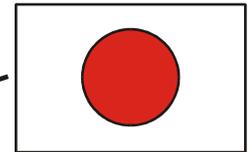
ISIS

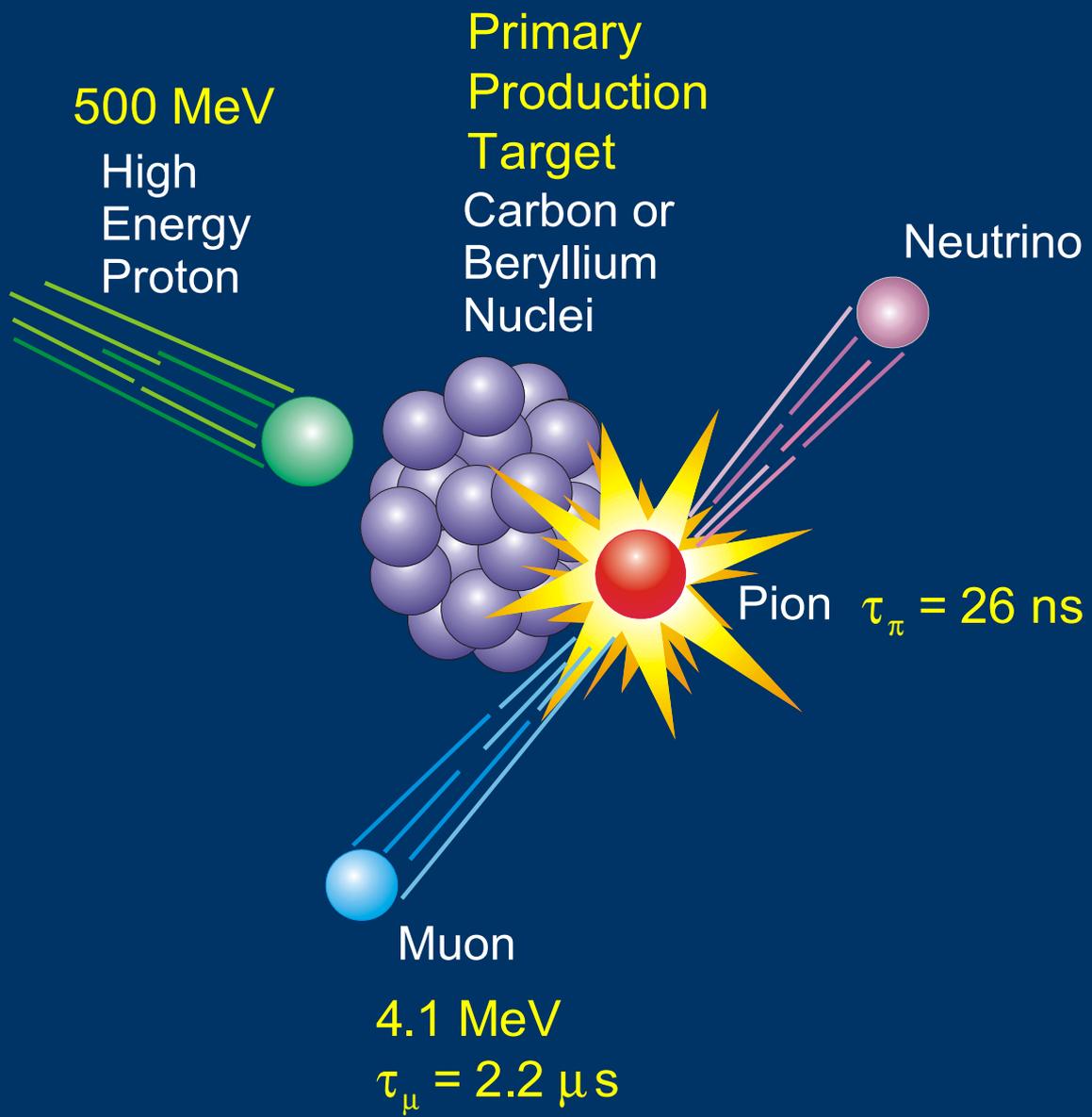


PSI



KEK





Pion Decay: $\pi^+ \rightarrow \mu^+ + \nu_\mu$

A pion **stops** in the “skin” of the primary production target.
It has zero linear momentum and zero angular momentum.

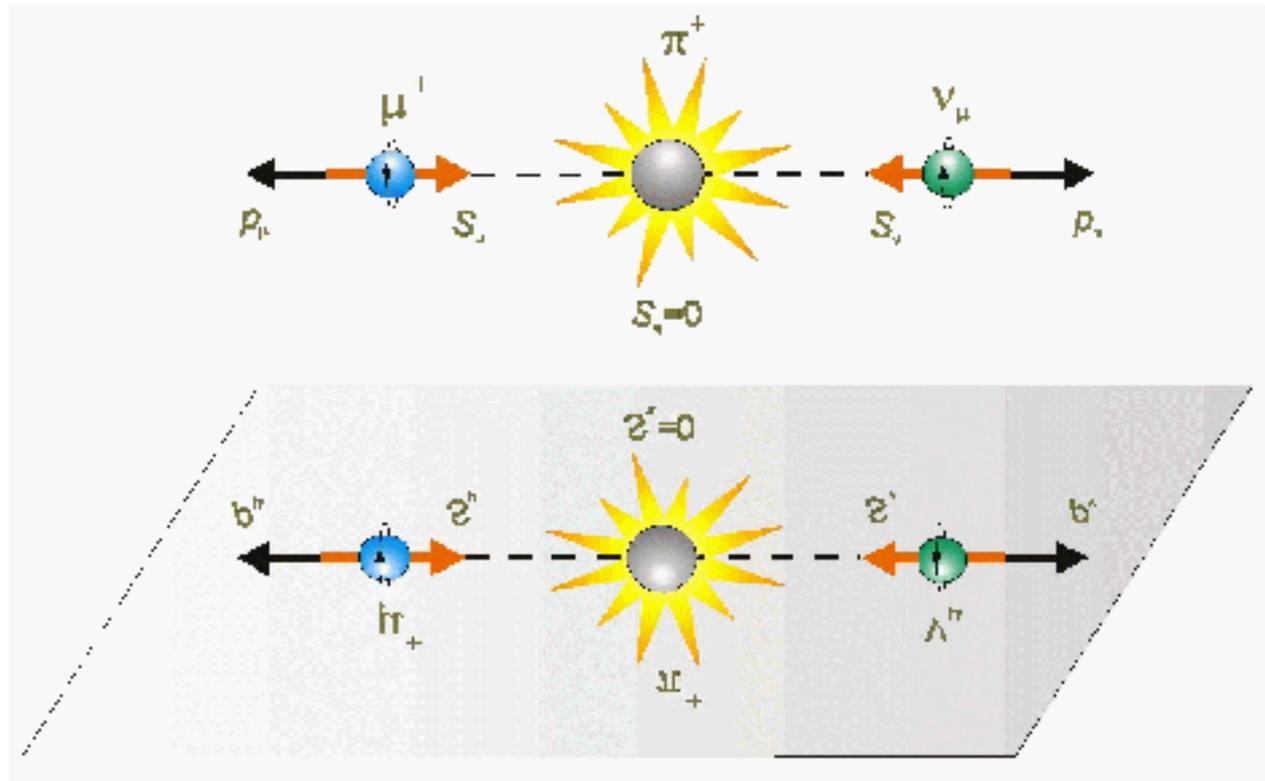
Conservation of Linear Momentum: The μ^+ is emitted with momentum equal and opposite to that of the ν_μ .

Conservation of Angular Momentum: μ^+ and ν_μ have equal and opposite spin.

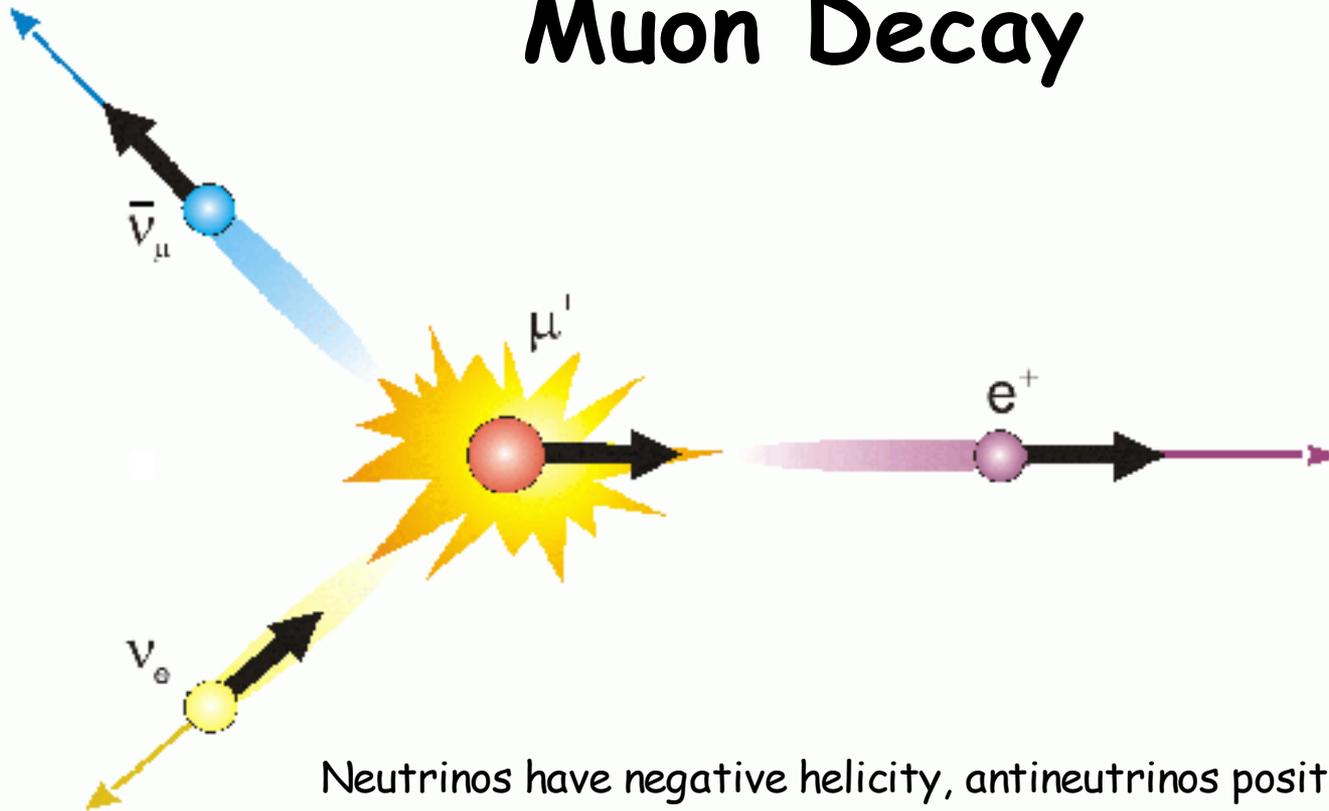
Weak Interaction:

Only “left-handed” ν_μ are created.

Thus the emerging μ^+ has its spin pointing *antiparallel* to its momentum direction.

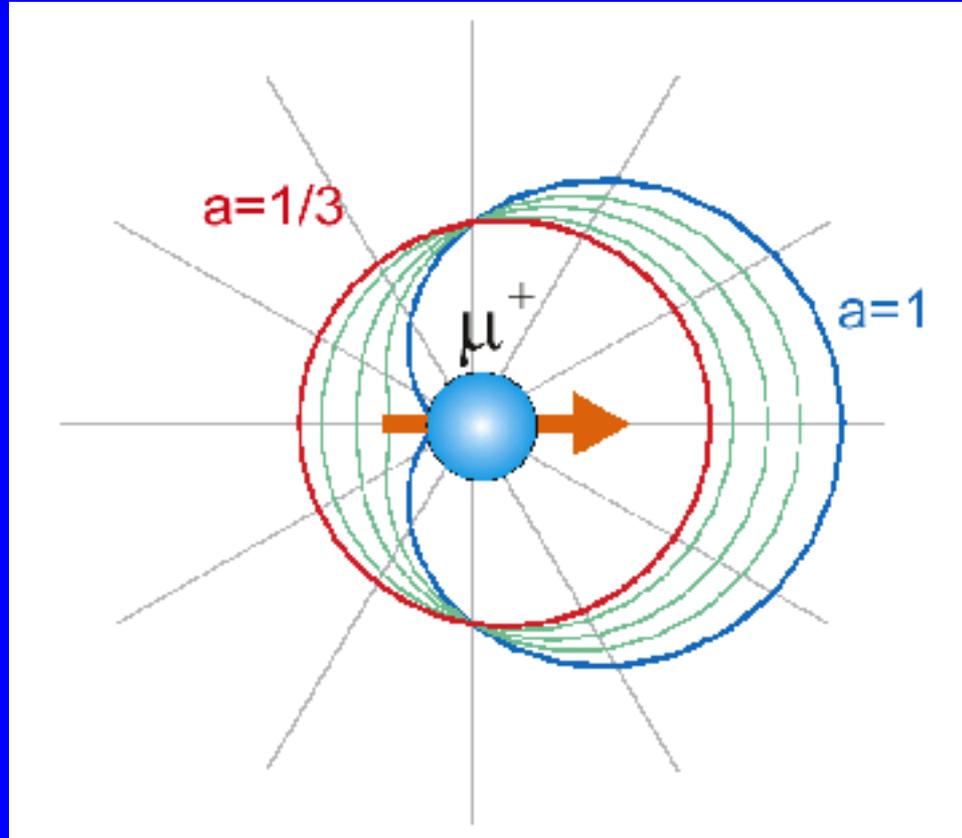


Muon Decay



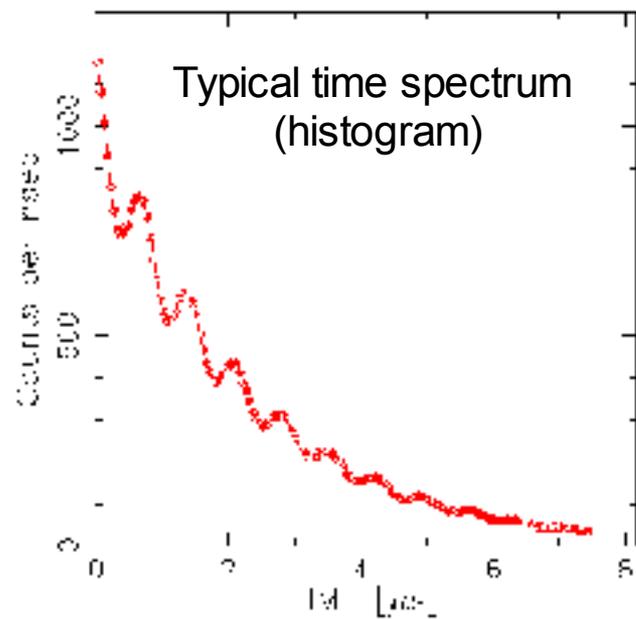
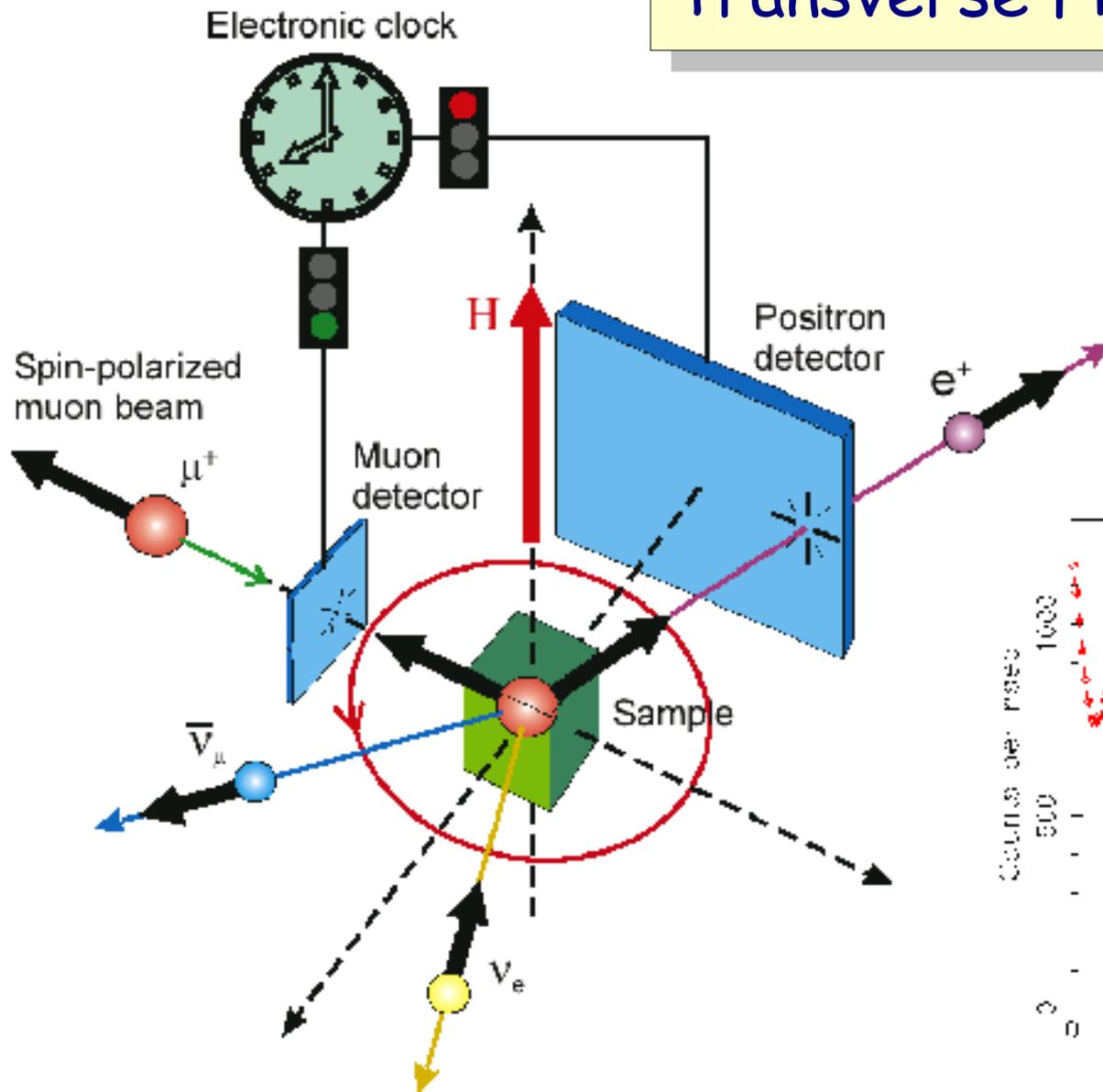
Neutrinos have negative helicity, antineutrinos positive.
An ultrarelativistic positron behaves like an antineutrino.
Thus the positron tends to be emitted along the muon spin
when ν_e and $\bar{\nu}_\mu$ go off together (highest energy e^+).

μ^+ Decay Asymmetry



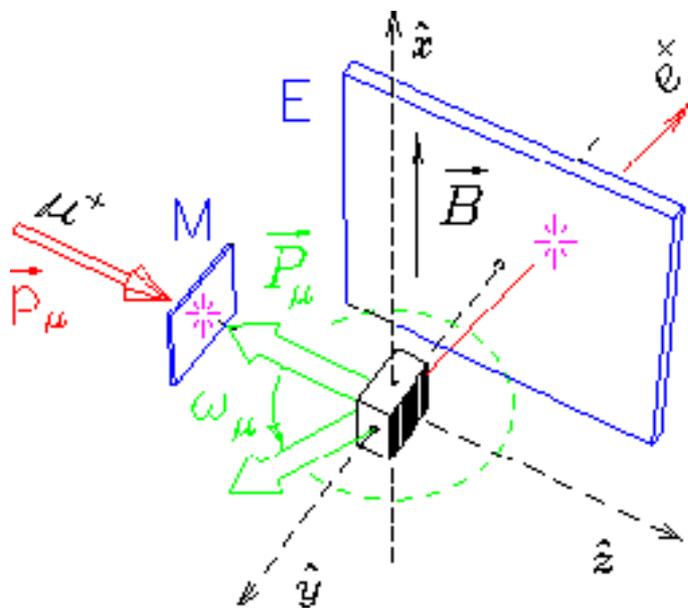
Angular distribution of positrons from μ^+ decay. The asymmetry is $a = 1/3$ when all positron energies are detected with equal probability.

Transverse Field (TF)- μ SR



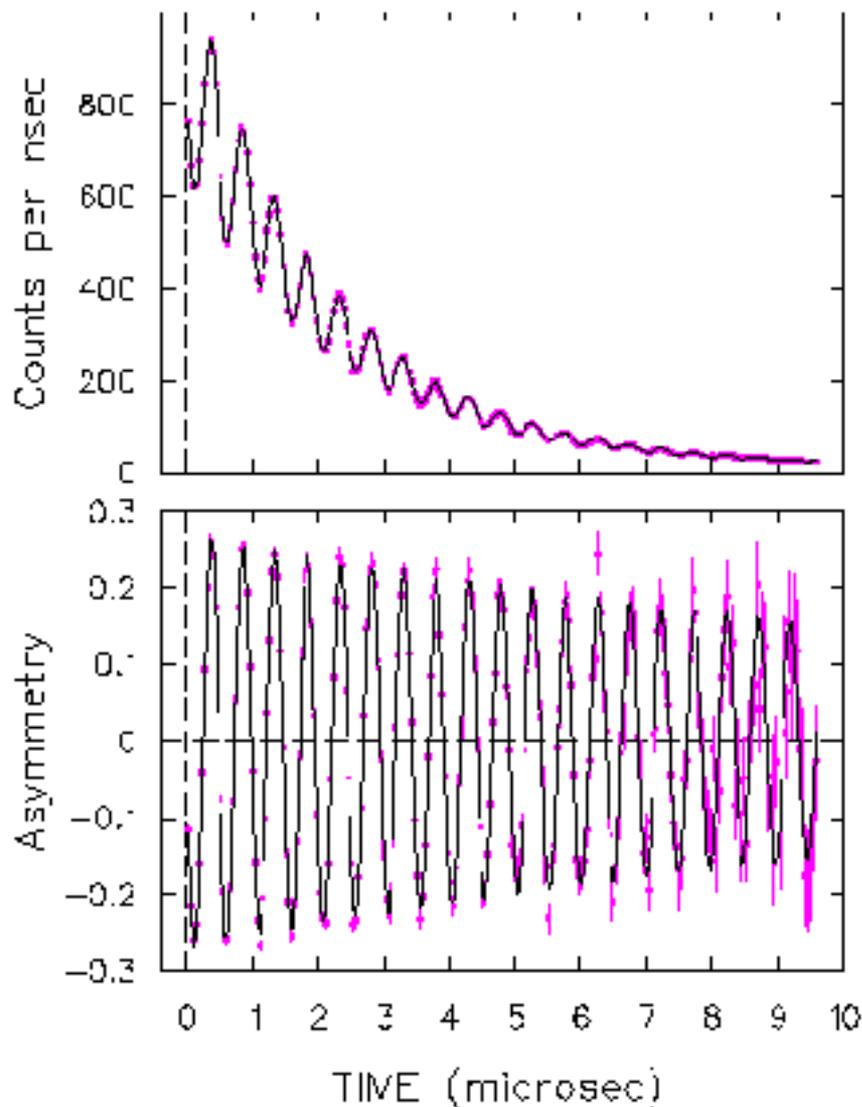
wTF- μ^+ SR:

$$N(t) = N_0 \left\{ \beta + e^{-t/\tau_\mu} [1 - A_0 G_{xx}(t) \cos(\omega_\mu t - \phi)] \right\}$$

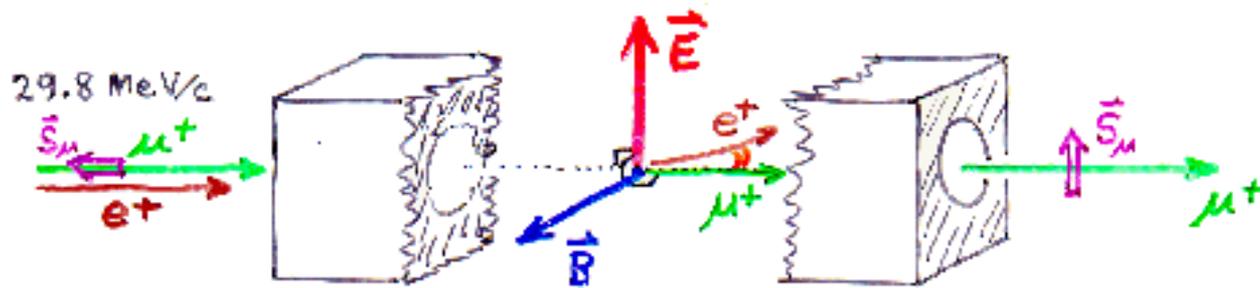


$$A(t) = [N(t) - N_0 \beta] e^{-t/\tau_\mu} - 1$$

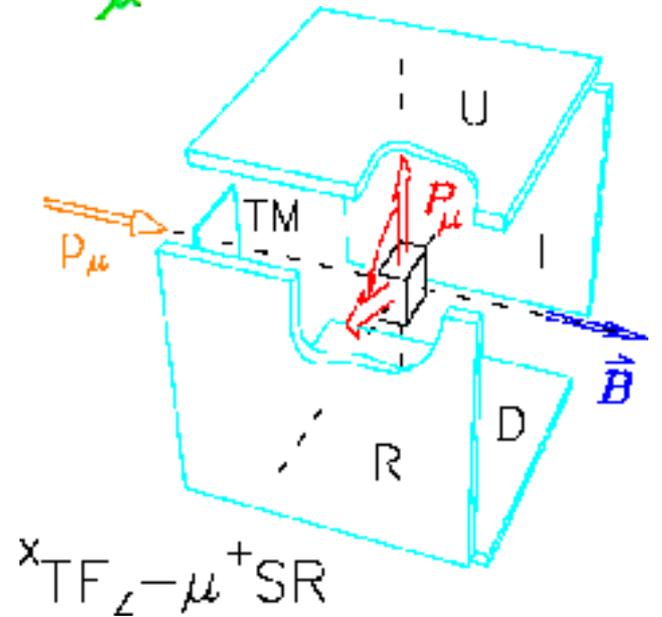
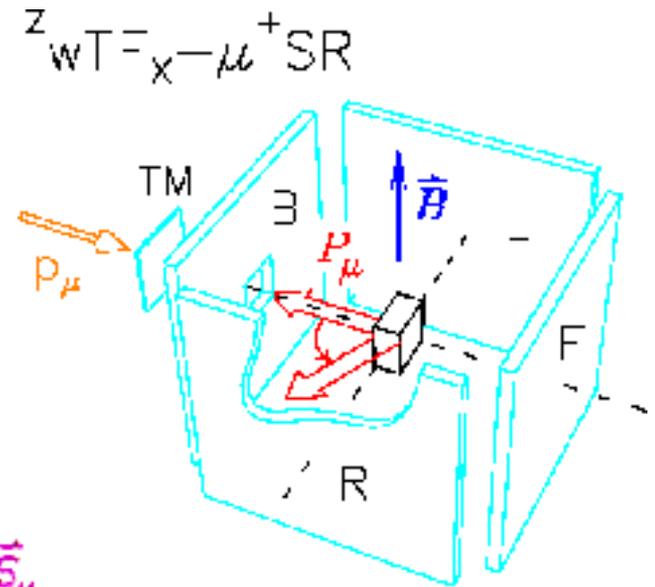
$$= A_0 G_{xx}(t) \cos(\omega_\mu t - \phi)$$



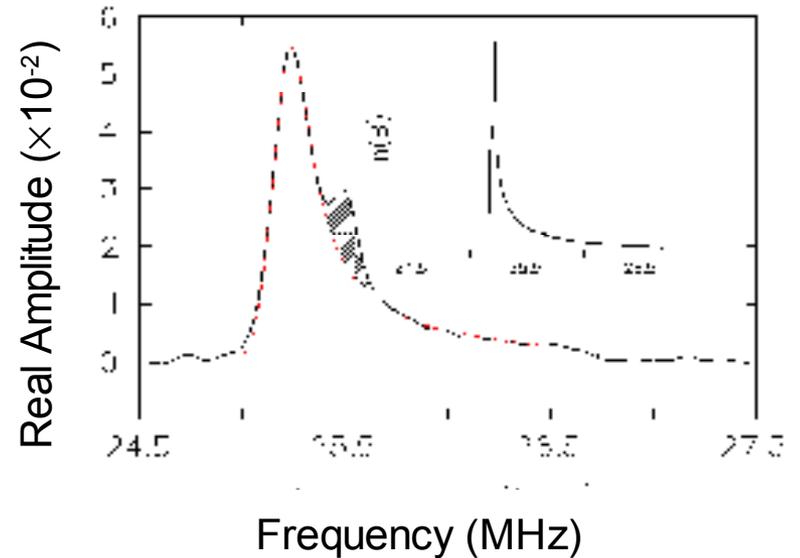
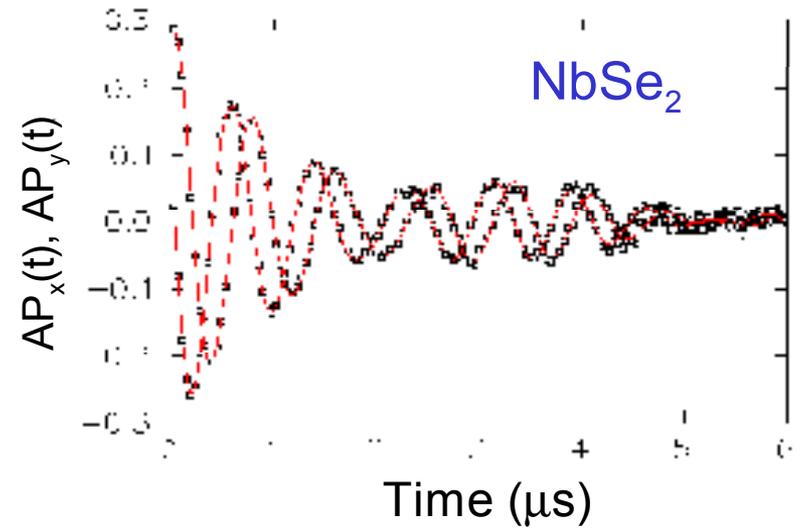
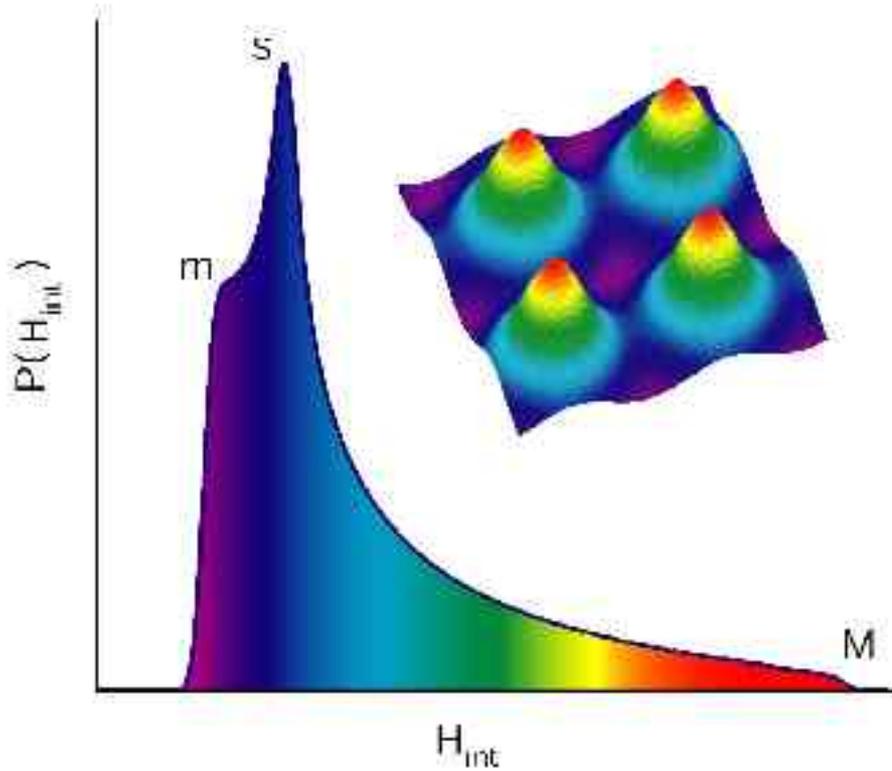
$E \times B$ velocity selector ("DC Separator" or Wien filter) for surface muons:



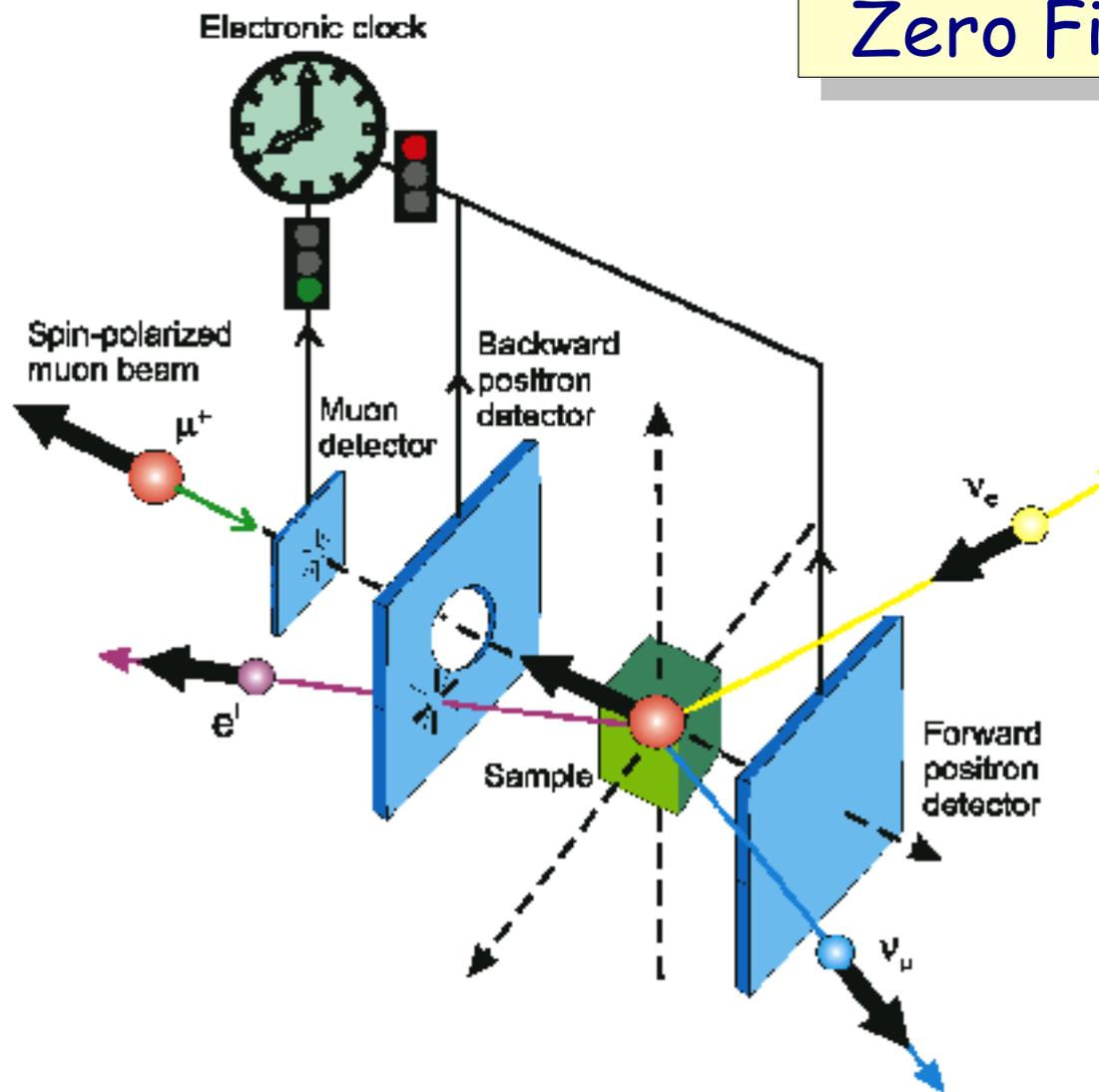
- Removes beam positrons
- Allows TF- μ^+ SR in high field (otherwise B deflects beam)



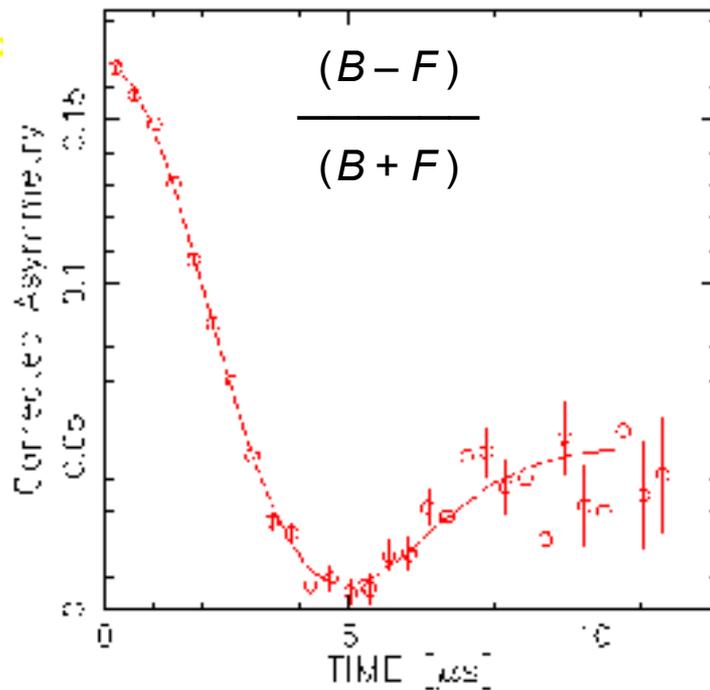
Magnetic Field Distribution of a Vortex Lattice



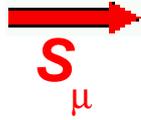
Zero Field (ZF)- μ SR



Typical asymmetry spectrum



Motion of Muon Spins in Static Local Fields:

 = Expectation value of one muon's spin direction

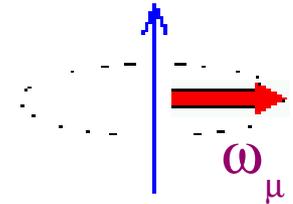
(a) All muons "see" same field \mathbf{B} :  for $\mathbf{B} \parallel \mathbf{S}_\mu$ nothing happens

$$\omega_\mu = 2\pi \gamma_\mu |\mathbf{B}|$$

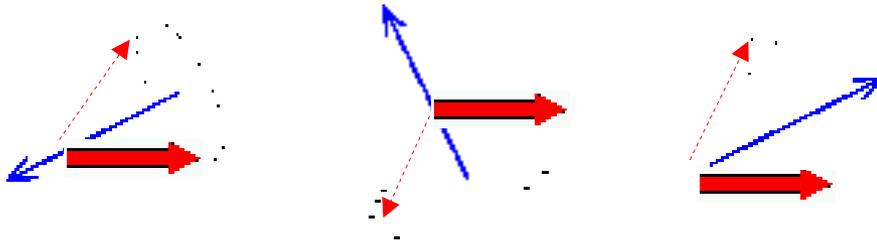
$$\gamma_\mu = 135.5 \text{ MHz/T}$$

for $\mathbf{B} \perp \mathbf{S}_\mu$ Larmor

precession:



(b) All muons "see" same $|\mathbf{B}|$ but **random direction**:



2/3 of \mathbf{S}_μ precesses at ω_μ

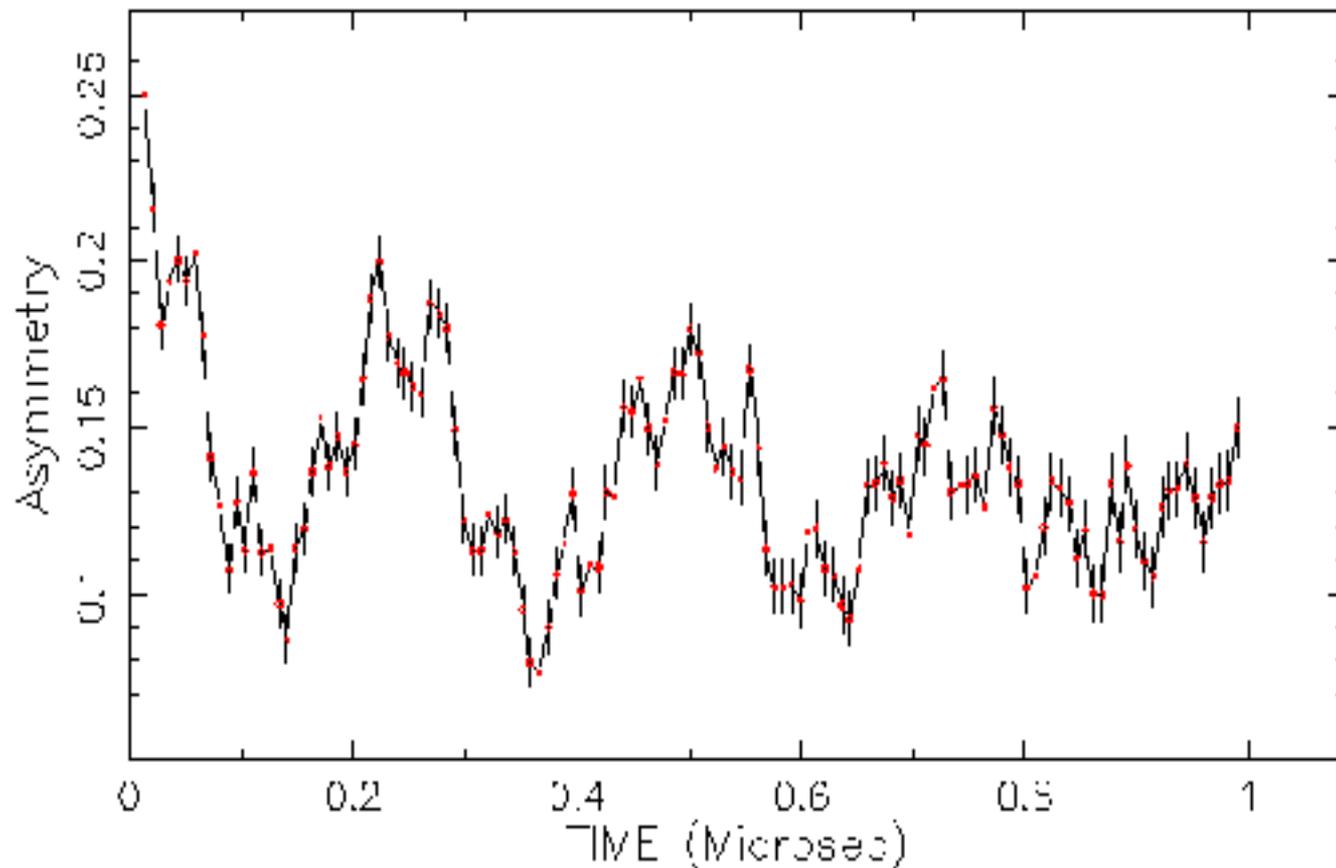
1/3 of \mathbf{S}_μ stays constant

(c) Local field \mathbf{B} **random** in both **magnitude** and **direction**:

All  do not return to the same orientation at the same time
(dephasing) $\Rightarrow \mathbf{S}_\mu$ "relaxes" as $G_{zz}(t)$ [Kubo & Toyabe, 1960's]

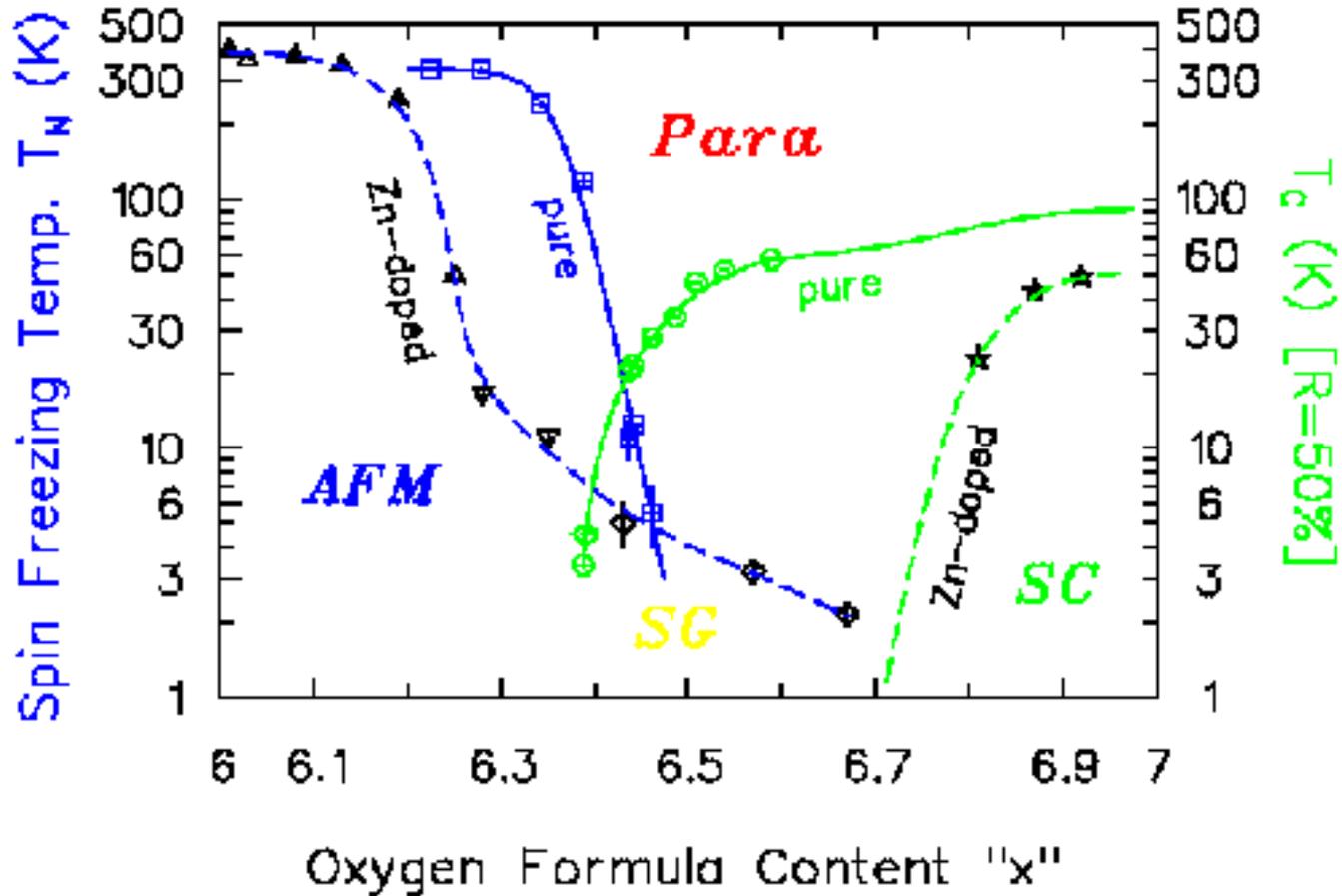
Antiferromagnetism in $\text{YBa}_2\text{Cu}_3\text{O}_{6.0}$ 1989

1164; GE or. $\text{YBa}_2\text{Cu}_3\text{O}_{6.0}$ Δ μ \perp \perp \perp $15.0(2)\text{K}$ [\uparrow vs \downarrow] ASY

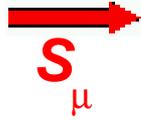


Phase Diagram of $\text{YBa}_2\text{Cu}_3\text{O}_x$

ca. 1990



Motion of Muon Spins in Static Local Fields:

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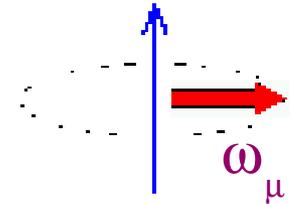
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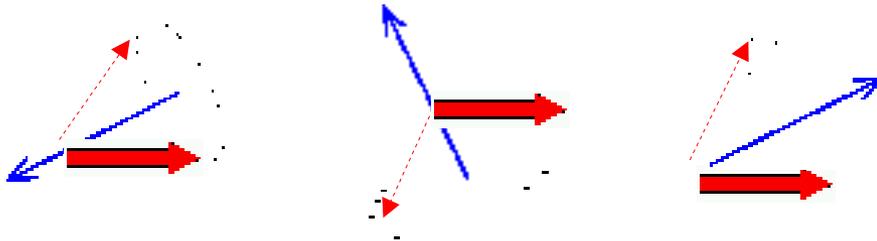
$$\gamma_\mu = 135.5 \text{ MHz/T}$$

for $\mathbf{B} \perp \mathbf{S}_\mu$ Larmor

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1/3 of \mathbf{S}_μ stays constant

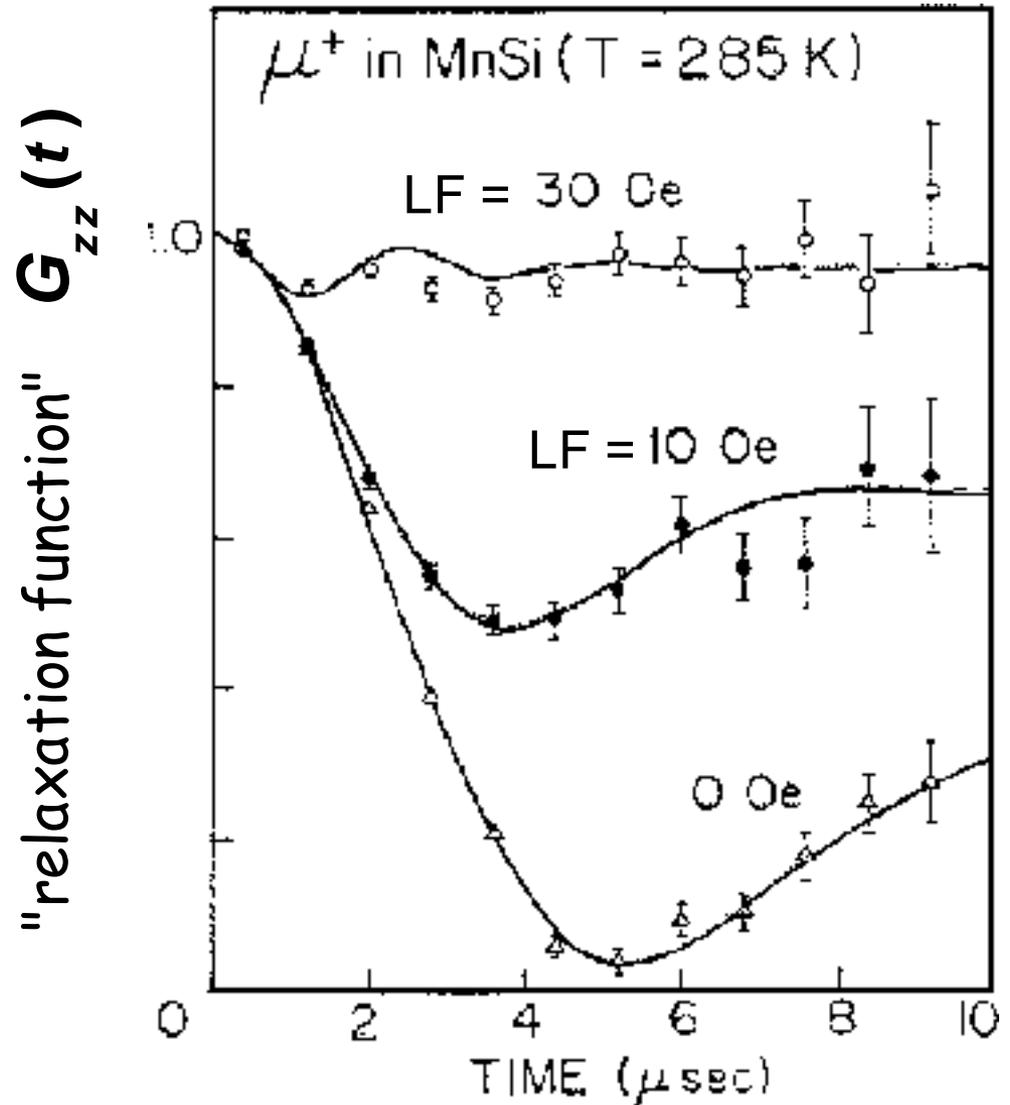
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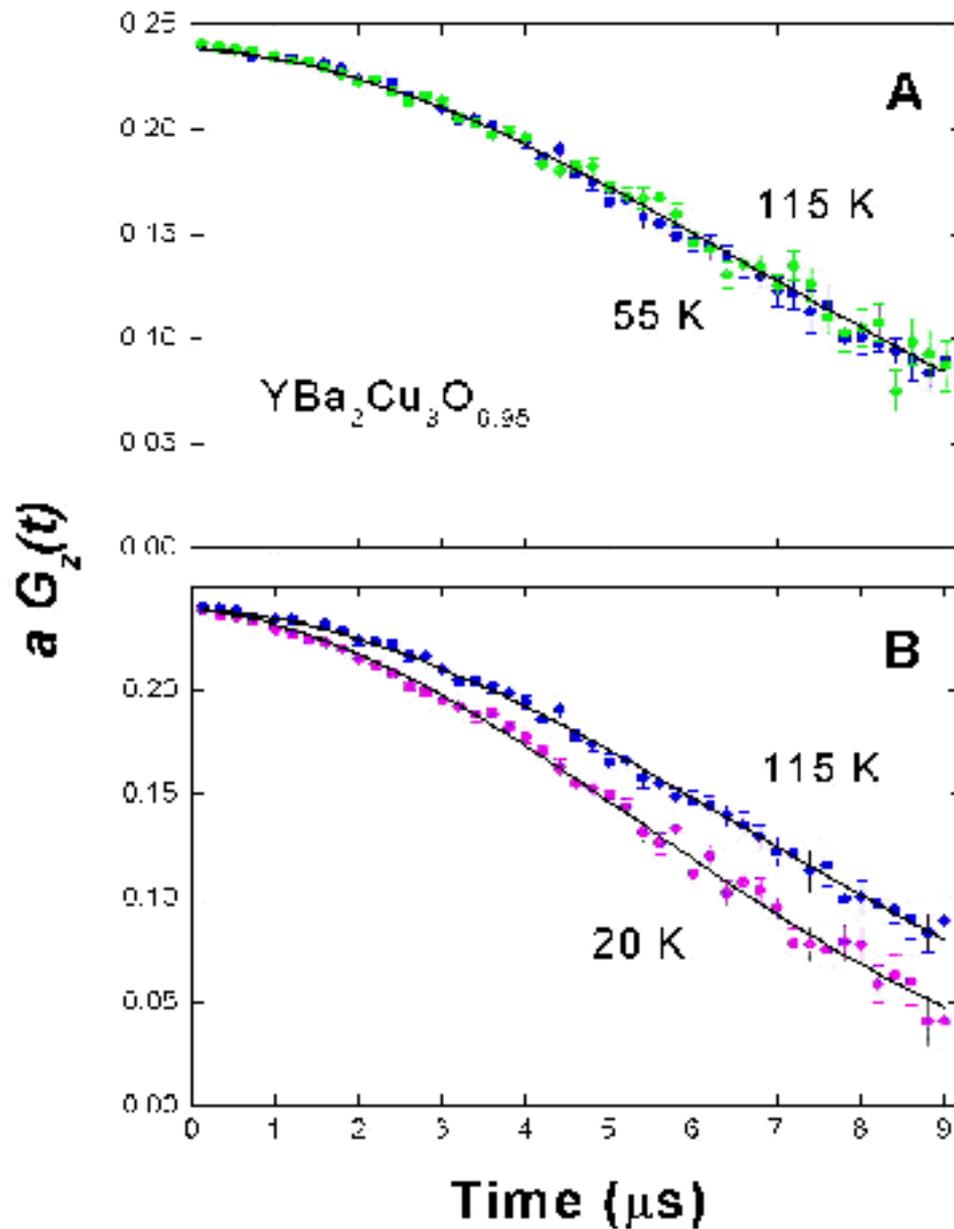
All  do not return to the same orientation at the same time
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ZF- μ^+ SR:

Kubo-Toyabe
Relaxation
due to
Nuclear
Dipolar Fields

Hayano, Uemura et al.,
1978



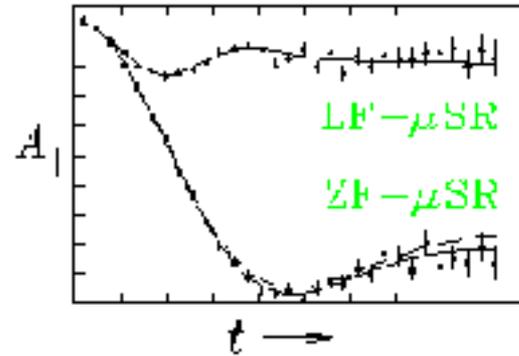
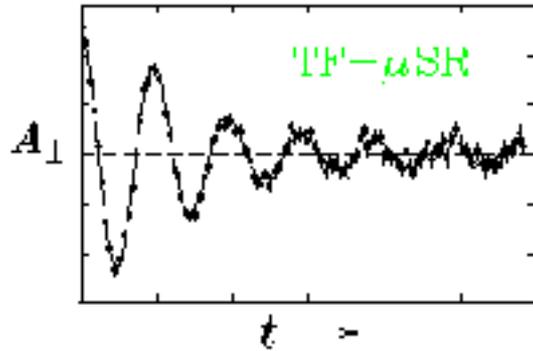


Sonier *et al.*,
 Science 292,
 1692 (2001)

"Extra"
 Magnetism
 at low T in
 $\text{YBa}_2\text{Cu}_3\text{O}_{6.95}$

Brewer's List of μ SR Acronyms

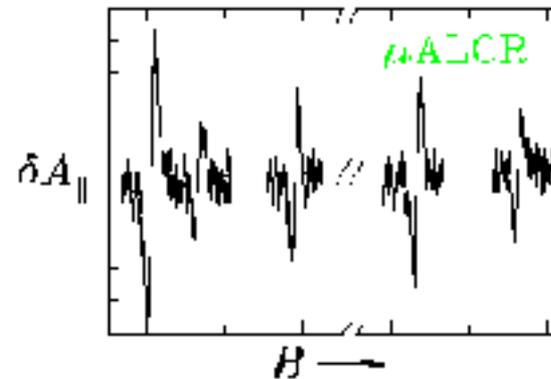
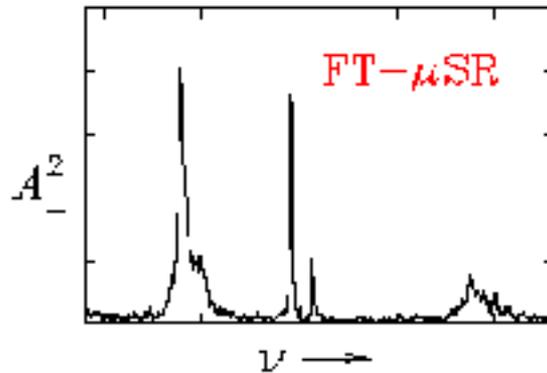
Transverse
Field



Longitudinal
Field

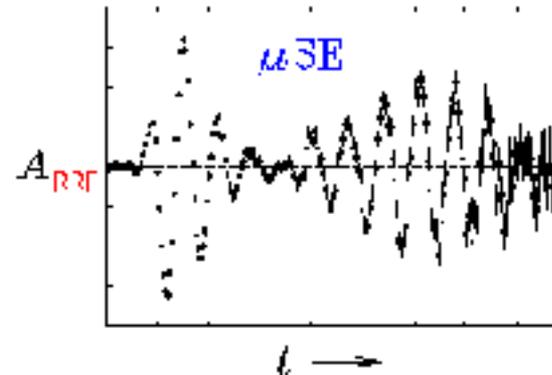
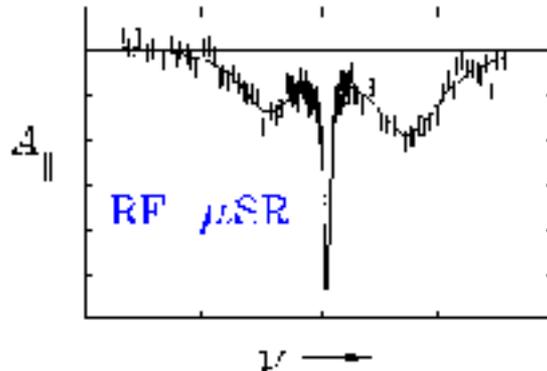
Zero Field

Fourier
Transform
 μ SR



Avoided
Level
Crossing
Resonance

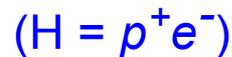
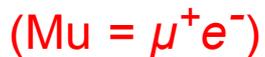
Muon
Spin
Resonance



Muon
Spin
Echo

"Themes" in μ^+ SR

Muonium as light Hydrogen



- **Mu** vs. **H** atom **Chemistry**:
 - gases, liquids & solids
 - Best test of reaction rate theories.
 - Study "unobservable" **H** atom rxns.
 - Discover new **radical** species.
- **Mu** vs. **H** in **Semiconductors**:
 - Until recently, μ^+ SR \rightarrow **only** data on metastable **H** states in semiconductors!
- **Quantum Diffusion**: μ^+ in metals (compare H^+); **Mu** in nonmetals (compare **H**).

The Muon as a Probe

- **Probing Magnetism**: unequaled sensitivity
 - Local fields: electronic structure; ordering
 - Dynamics: electronic, nuclear spins
- **Probing Superconductivity**: (esp. HT_cSC)
 - Coexistence of SC & Magnetism
 - Magnetic Penetration Depth λ
 - Coherence Length ξ

End of Introduction!

Ask Questions?

Take a break?

Vote on Part II:

- (1) μ^-SR
- (2) $TF-\mu^+SR$ in Superconductors: Vortex Lattice
- (3) $ZF-\mu^+SR$ in Superconductors: Magnetism
- (4) μ^+ and Muonium States in Nonmetals
- (5) Nothing (end early)